## UNSCENTED KALMAN FILTERING FOR GREENHOUSE CLIMATE CONTROL SYSTEMS WITH MISSING MEASUREMENT

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ABSTRACT. A stochastic unscented Kalman filter is designed in an attempt to solve the state estimation problem of the greenhouse climate control systems with missing measurements. The missing measurements are described by a binary switching sequence satisfying a conditional probability distribution. In order to accommodate the effects of randomly varying arrival of measurement data, the stochastic unscented transformation coupled with certain parts of the classic Kalman filter is applied to estimate the greenhouse states and filter out the noises, where some or all measurements are lost in a random fashion. The simulation results demonstrate the performance degradation of state estimation caused by random measurement data loss.

Keywords: Unscented Kalman filter, Greenhouse, Nonlinear systems, State estimation

1. Introduction. The greenhouse climate control system is a very complex dynamic system covered with thin and transparent materials. This system satisfies the conditions for plant growth, but creates difficulties in regulating the greenhouse environment because of highly coupled nonlinear dynamics and strong disturbances from the surroundings, such as global radiation, wind speed and direction, and external air temperature and humidity. In order to create a favorable environment to accelerate the crop development and to minimize the production costs in terms of raw materials and energy consumption, researchers have used a wide variety of control techniques in different fields, from the conventional or classic strategies (pole placement control and linear quadratic regulation [1,2]), intelligent control algorithms (fuzzy logic, neural networks, genetic algorithms [3-6]), advanced control techniques (predictive control, adaptive control [7,8]), to robust control strategies [9], no-linear and optimal control [10,11], and fault detection and isolation in greenhouse [12]. It is well known that, the most advanced control structures, ensuring very good performance of the system, are based on control structures with additional feedback from system state variables, such as temperature and humidity in greenhouse. Therefore, acceptable control of the greenhouse climate systems requires the accurate estimation of the states variables.

On the other hand, the efficiency of plant production in greenhouses relies on the measurements provided by several electronic sensors located inside and outside the greenhouse. Environmental conditions such as the direct exposure of sensors to sunlight and the deterioration of connections between sensors and the controllers could result in very noisy and incomplete measurements which may impair the greenhouse operation. It may also increase the number of false alarms received from fault detection and isolation systems.

To ensure the accurate state estimation, it is necessary to develop a suitable filtering technique to filter out the noises and estimate the states of greenhouses. However, to the best of our knowledge, the important state estimation problem for greenhouse climate control systems with noises has not been reported in the literature.

It is well known that the optimal filter for linear systems is the Kalman filter [13-19]. State estimation for nonlinear systems is a difficult problem, and the extended Kalman filter (EKF) can cope with some nonlinear systems by using linearization of the state equation around the predicted state. Although the EKF is a widely used filtering strategy, and has been used successfully in many applications [20-22], in practice, the derivation of the Jacobian matrices is nontrivial and often leads to significant implementation difficulties. What is more, linearization can produce highly unstable filters if the assumption of local linearity is violated.

A recent improvement to the EKF is the unscented Kalman filter (UKF). The UKF is a nonlinear filter, and was first proposed by Julier and Uhlmann [23]. This filter is more accurate than the EKF and easier to implement for nonlinear systems without the linearization steps required by the EKF. So the UKF has found a number of applications in high-order nonlinear complex systems, including navigation systems for high-speed road, public transformation systems, underwater vehicles, and target tracking, etc. [24-26].

The ability of the UKF to accurately estimate nonlinearities makes it attractive for implementation on greenhouse climate control systems. This paper represents the first attempt to apply the UKF to estimate the states and filter out the noises of greenhouse climate control systems with missing measurement, which are described by a binary switching sequence satisfying a conditional probability distribution. General simulation results are given and a brief comparison is made between state estimation performance of the UKF with and without measurement data loss.

In the next section, a more detailed description about the operation of the UKF is given. In Section 3, the model of greenhouse climate control system configured for UKF is presented and analyzed. Section 4 investigates the simulation results of the UKF and makes a comparison between the performance of the UKF with and without measurement data loss. Conclusions about the results are summarized in Section 5.

2. Unscented Kalman Filter. The UKF was developed with the underlying assumption that approximating a Gaussian distribution is easier than approximating a nonlinear transformation [27]. The fundamental component of UKF is the unscented transformation, which uses a set of samples, or sigma points to capture the true mean and covariance of the state probability distribution. These sigma points undergo the nonlinear transformation. The posterior mean and covariance of the state are then calculated from the transformed sigma points. This approach gives the UKF better convergence characteristics and greater accuracy than the EKF for nonlinear systems.

Suppose the nonlinear system equations obey the following nonlinear relationships:

$$\begin{cases} x(k+1) = f(x(k), u(k), k) + w(k) \\ y(k) = h(x(k)) + v(k) \\ z(k) = \alpha(k)y(k) \end{cases}$$
(1)

where x(k) is the state vector, u(k) is the control input, y(k) is the raw measurement vector, z(k) is the received measurement vector, w(k) is the process noise vector assumed to be additive, white, and Gaussian, with zero mean and covariance defined as Q, v(k) is the measurement noise vector defined the same as w(k) but with the different covariance R, and  $\alpha(k)$  is a Bernoulli distributed white sequence with

$$Prob \{ \alpha(k) = 1 \} = E \{ \alpha(k) \} = \bar{\alpha} Prob \{ \alpha(k) = 0 \} = 1 - E \{ \alpha(k) \} = 1 - \bar{\alpha}$$

First of all, the filter is initialized with the following assumptions for the state estimate x(0) and the error covariance matrix P(0)

$$\hat{x}^{+}(0) = E[x(0)] \tag{2}$$

$$P^{+}(0) = E\left[\left(x(0) - \hat{x}^{+}(0)\right)\left(x(0) - \hat{x}^{+}(0)\right)^{T}\right]$$
(3)

Then, the following time update equations are used to propagate the state estimation and covariance for every measurement  $k \in \{1, 2, \dots, \infty\}$ :

1. Calculation of the sigma points from the initial conditions (2) and (3)

$$\hat{x}^{(i)}(k-1) = \hat{x}^{+}(k-1) + \tilde{x}^{(i)}, \quad i = 1, 2, \cdots, 2n$$

$$\tilde{x}^{(i)} = \left(\sqrt{nP^{+}(k-1)}\right)_{i}, \quad i = 1, 2, \cdots, n$$

$$\tilde{x}^{(n+i)} = -\left(\sqrt{nP^{+}(k-1)}\right)_{i}, \quad i = 1, 2, \cdots, n$$
(4)

2. Transformation of these sigma points using Equation (1)

$$\hat{x}^{(i)}(k) = f\left(\hat{x}^{(i)}(k-1), u(k-1), k-1\right)$$
(5)

3. Combine the  $\hat{x}^{(i)}(k)$  vectors to obtain the prediction of the state estimate

$$\hat{x}(k) = \frac{1}{2n} \sum_{i=1}^{2n} \hat{x}^{(i)}(k)$$
(6)

4. As the process noise is addictive and independent, the predicted error covariance is given as

$$P(k) = \frac{1}{2n} \sum_{i=1}^{2n} \left( \hat{x}^{(i)}(k) - \hat{x}(k) \right) \left( \hat{x}^{(i)}(k) - \hat{x}(k) \right)^T + Q \tag{7}$$

Finally, implement the following measurement update eauations:

1. Updating the sigma points with the predicted mean and covariance

$$\hat{x}^{(i)}(k) = \hat{x}^{+}(k) + \tilde{x}^{(i)}, \quad i = 1, 2, \cdots, 2n 
\tilde{x}^{(i)} = \left(\sqrt{nP(k)}\right)_{i}, \quad i = 1, 2, \cdots, n 
\tilde{x}^{(n+i)} = -\left(\sqrt{nP(k)}\right)_{i}, \quad i = 1, 2, \cdots, n$$
(8)

2. Transformation of each of the predicted points through measure equation

$$\hat{y}^{(i)}(k) = \alpha(k)h(\hat{x}^{(i)}(k), k)$$
(9)

3. Combine the  $\hat{y}^{(i)}(k)$  vectors to obtain the predicted measure

$$\hat{y}(k) = \frac{1}{2n} \sum_{i=1}^{2n} \hat{y}^{(i)}(k)$$
(10)

4. Since the measurement noise is also addictive and independent, the covariance of the predicted measurement is as follows:

$$P_y(k) = \frac{1}{2n} \sum_{i=1}^{2n} \left( \hat{y}^{(i)}(k) - \hat{y}(k) \right) \left( \hat{y}^{(i)}(k) - \hat{y}(k) \right)^T + R \tag{11}$$

5. Estimate the covariance between  $\hat{x}(k)$  and  $\hat{y}(k)$ 

$$P_{xy}(k) = \frac{1}{2n} \sum_{i=1}^{2n} \left( \hat{x}^{(i)}(k) - \hat{x}(k) \right) \left( \hat{y}^{(i)}(k) - \hat{y}(k) \right)^T$$
(12)

6. The measurement updates are performed as follows:

$$K(k) = P_{xy}(k)P_{y}^{-1}(k)$$
(13)

$$\hat{x}^{+}(k) = \hat{x}(k) + K(k) \left(\alpha(k)y(k) - \hat{y}(k)\right)$$
(14)

$$P^{+}(k) = P(k) - K(k)P_{y}(k)K^{T}(k)$$
(15)

where y(k) is the measurement.

**Remark 2.1.** Stochastic variable  $\alpha(k)$  is used to indicate the effects of randomly varying arrival of measurement data. That is, if  $\alpha(k) = 1$ , then no measurement data lost in the system, and if  $\alpha(k) < 1$ , part or all of the measurement data are lost.

**Remark 2.2.** The choice of the covariance matrices Q and R has affect on the quality of the state estimation. However, according to the existing technical literature, the analytical guidelines which ensure proper settings of matrices do not exist. In this paper, the trial and error procedure is used. Therefore, a future subject of this study is to develop an optimization procedure, such as the genetic algorithm, to set the covariance matrices Q and R to ensure the optimal settings of UKF parameters.

**Remark 2.3.** Note that no explicit calculation of Jacobians is necessary to implement this algorithm, which reduces the complexity and errors associated with finding the Jacobians of a complex system and also allows the filter to be applied to a wide scope of system formulations.

3. Greenhouse Climate Control Dynamics. The dynamic changes in the greenhouse are determined by differences in energy and mass contents between inside and outside air. In a greenhouse, the state climate can be represented by two variables, namely, inside air temperature, and absolute humidity. A simplified greenhouse climate model adequate for control purposes describes the dynamic behavior of the state variable with the following energy balance and water vapor balance equations [28].

3.1. Energy balance. The greenhouse air energy balance is affected by energy supply and energy losses. The former is due to an artificial heating system  $(E_h)$  and heat load imposed by solar radiation  $(E_s)$  and the latter is due to transmission through the greenhouse cover  $(E_c)$ , forced ventilation  $(E_v)$ , and fog system  $(E_f)$ . This balance can be written as follows:

$$\frac{dT_{in}}{dt} = \frac{1}{C_0} \left( E_h - E_c - E_v - E_f + E_s \right)$$
(16)

in which,

$$E_{h} = Q_{heater}, \quad E_{s} = S_{i}, \quad E_{v} = \frac{V_{R}C_{0}}{V_{T}} \left(T_{in} - T_{out}\right)$$
$$E_{c} = UA \left(T_{in} - T_{out}\right), \quad E_{f} = \lambda Q_{fog}$$

where  $T_{in}/T_{out}$  is the inside/outside air temperature,  $C_0$  is the thermal capacity,  $Q_{heater}$  is the heat provided by the greenhouse heater,  $S_i$  is the intercepted solar radiant energy,  $V_R$ is the ventilation rate, UA is the heat transfer coefficient of enclosure,  $\lambda$  is the latent heat of vaporization,  $Q_{fog}$  is the water capacity of the fog system, and  $V_T$  is the temperature active mixing air volume.

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3.2. Water vapor balance. The water vapor balance is calculated by the following formula, modified according to [29], in which the soil evaporation rate and the condensation rate at the inner face of the greenhouse cover are neglected:

$$\frac{dw_{in}}{dt} = \frac{1}{V_H} \left( Q_{fog} + E(S_i, w_{in}) - V_R \left( w_{in} - w_{out} \right) \right)$$
(17)

where  $w_{in}/w_{out}$  is the inside/outside humidity,  $E(S_i, w_{in})$  is the evapotranspiration rate of the plants, and  $V_H$  is the humidity active mixing air volume.

In summer operation,  $Q_{heater}$  is set to zero. It is also worth noticing that, the evapotranspiration rate  $E(S_i, w_{in})$  is related to the intercepted solar radiant energy through the following simplified relation:

$$E(S_i, w_{in}) = \alpha \frac{S_i}{\lambda} - \beta_T w_{in} \tag{18}$$

where  $\alpha$  is an overall coefficient to account for shading and leaf area index and  $\beta_T$  is an overall coefficient to account for thermodynamic constants and other factors affecting evapotranspiration (i.e., stomata, air motion).

3.3. Dynamic model of the greenhouse climate control systems. In paper [11], considering that the conditions of operating the ventilation-cooling are rather dominated by solar radiation alone (i.e.,  $\beta_T = 0$ ), the term  $\beta_T w_{in}$  can be neglected. Supposing  $\alpha' = \alpha (\lambda V_H)^{-1}$ , normalizing the control variables through these equations  $V_{R,\%} = V_R/V_R^{\max}$ ,  $Q_{fog,\%} = Q_{fog}/Q_{fog}^{\max}$ ,  $\lambda' = \lambda Q_{fog}^{\max}$ ,  $V' = V_H/Q_{fog}^{\max}$ , and defining the inside temperature and humidity as the dynamic state variables,  $x_1$  and  $x_2$ , respectively, the ventilation rate and the water capacity of the fog system as the control (actuator) variables,  $u_1$  and  $u_2$ , respectively, the intercepted solar radiant energy, the outside temperature, and the outside absolute humidity as the disturbances,  $z_i(t)$ , i = 1, 2, 3, and  $y = x_1^2 + x_2^2$ , Equations (16) and (17) can be put in the following state-space form:

$$\begin{cases} \dot{x}_{1} = \frac{1}{C_{0}} \left( z_{1} - \lambda' u_{2} \right) - \frac{u_{1}}{t_{v}} \left( x_{1} - z_{2} \right) - \frac{UA}{C_{0}} \left( x_{1} - z_{2} \right) \\ \dot{x}_{2} = \frac{1}{V'} u_{2} + \alpha' z_{1} - \frac{u_{1}}{t_{v}} \left( x_{2} - z_{3} \right) \\ y = x \end{cases}$$

$$(19)$$

where parameter  $t_v$  represents the time needed for one air change the sampling period.

The UKF algorithm is designed for the discrete time system. So we should discretize the above continuous-time model to apply the algorithm. In this paper, the nonlinear 3-order Runge-Kutta algorithm is applied to discretize the model (19) with a proper simulation step (1s).

**Remark 3.1.** It should be pointed out that if some international standards are used to protect the systems against the external environment, such as IP 55, IP 65, etc., and a good maintenance is performed, then the influence of system noise can be neglected. In this case, the UKF algorithm can be removed.

4. Simulation Results. In the simulation, the greenhouse model parameters described in (19) are as follows [11]:

$$C_0 = -324.67 \min W \, {}^{o}C^{-1}, \quad UA = 29.8 W \, {}^{o}C^{-1}, \quad t_v = 3.41 \min \\ \lambda' = 465 W, \quad \alpha' = 0.0033 g \, m^{-3} \min^{-1} W^{-1}, \quad 1/V' = 13.3 g \, m^{-3} \min^{-1} M^{-1}$$

The UKF was designed for the state estimation problem, and has been applied in nonlinear control applications requiring full-state feedback [30]. In this paper, we use a

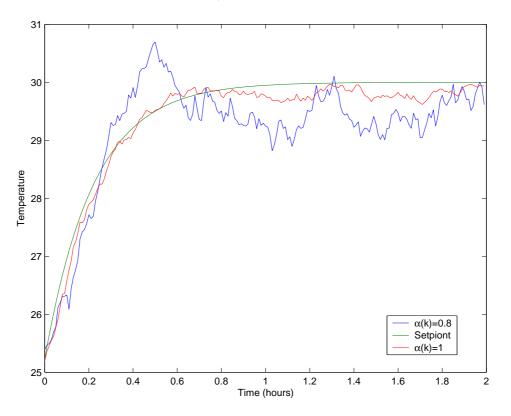


FIGURE 1. Temperature response in greenhouse

nonlinear control technique proposed in [11] to control the above model, and put emphasis on the estimation performance of the state from the noisy measurement.

Assume  $\alpha(k) = 0.8$ , and the Gaussian white noise w(k) and v(k) are added to both the process and measurement equations to simulate the real situation

$$E[w(k)] = \begin{bmatrix} 0 & 0 \end{bmatrix}^T, \quad E[v(k)] = \begin{bmatrix} 0 & 0 \end{bmatrix}^T$$
$$Q = diag(\begin{bmatrix} 10^{-6} & 10^{-6} \end{bmatrix}) \quad R = diag(\begin{bmatrix} 0.5 & 0.5 \end{bmatrix})$$

This paper tries to describe a kind of filtering technique for the practical application at greenhouse climate control system to estimate the temperature and humidity. Simulation results are illustrated from Figure 1 to Figure 2, which show the results of the temperature and humidity estimation by UKF with and without measurement loss, respectively.

By comparison from Figure 1 to Figure 2, it can be seen that the UKF algorithm without considering missing measurement gives a more accurate and smoother estimation than the one with measurement loss.

5. **Conclusion.** This paper presents a derivative-free nonlinear filtering technique to the state estimation problem for greenhouse climate control systems. It has been shown that the UKF algorithm without considering missing measurement achieves a better level of accuracy than the one with measurement loss. This simulation result will be very useful for further study of state estimation of greenhouse climate control systems with communication constraints.

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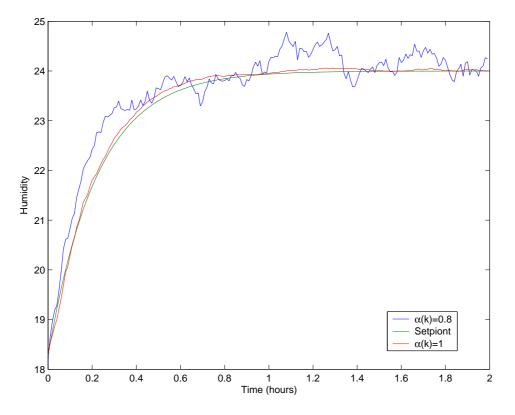


FIGURE 2. Humidity response in greenhouse

## REFERENCES

- B. Anderson and R. Johnstone, Global adaptive pole positioning, *IEEE Transactions on Automatic Control*, vol.30, no.1, pp.11-22, 1985.
- [2] N. A. Sigrimis, K. G. Arvanitis and R. S. Gates, A learning technique for a general purpose optimizer, Computers and Electronics in Agriculture, vol.26, no.2, pp.83-103, 2000.
- [3] R. L. Fortuna, G. Nunnari, L. Occhipinti and M. G. Xibilia, Soft computing for greenhouse climate control, *IEEE Transactions on Fuzzy Systems*, vol.8, no.6, pp.753-760, 2000.
- [4] A. Y. Idirek and F. L. Lewis, Feedback linearization using neural networks, Automatica, vol.31, no.11, pp.1659-1664, 1995.
- [5] S. Jagannathan, S. Commuri and F. L. Lewis, Feedback linearization using CMAC neural networks, *Automatica*, vol.34, no.5, pp.547-557, 1998.
- [6] F. Fourati and M. Chtourou, A greenhouse neural control using generalized and specialized learning, International Journal of Innovative Computing, Information and Control, vol.7, no.10, pp.5813-5824, 2011.
- [7] M. Y. El Ghoumari, H. J. Tantau and J. Serrano, Non-linear constrained MPC: Real-time implementation of greenhouse air temperature control, *Computers and Electronics in Agriculture*, vol.49, pp.345-356, 2005.
- [8] F. Rodriguez, J. L. Guzman, M. Berenguel and M. R. Arahal, Adaptive hierarchical control of greenhouse crop production, Int. J. Adap. Cont. Signal Process., vol.22, pp.180-197, 2008.
- [9] N. Bennis, J. Duplaix, G. Enea, M. Haloua and H. Youlal, Greenhouse climate modelling and robust control, computers and electronics in agriculture, *Computers and Electronics in Agriculture*, vol.61, pp.96-107, 2008.
- [10] E. J. V. Henten, Sensitivity analysis of an optimal control problem in greenhouse climate management, *Biosystems Engineering*, vol.85, pp.355-364, 2003.
- [11] G. Pasgianos, K. Arvanitis, P. Polycarpou and N. Sigrimis, A nonlinear feedback technique for greenhouse environmental control, *Computers and Electronics in Agriculture*, vol.40, pp.153-177, 2003.
- [12] R. Linker, P. O. Gutman and I. Seginer, Robust model-based failure detection and identification in greenhouses, *Computers and Electronics in Agriculture*, vol.26, no.3, pp.255-270, 2000.

- [13] M. Mahmoud and P. Shi, Robust Kalman filtering for continuous time-lag systems with Markovian jump parameters, *IEEE Transactions on Circuits and Systems*, vol.50, no.1, pp.98-105, 2003.
- [14] H. Palangi and M. H. Refan, Error reduction of a low cost GPS receiver for kinematic applications based on a new Kalman filtering algorithm, *International Journal of Innovative Computing*, *Information and Control*, vol.6, no.8, pp.3775-3786, 2010.
- [15] M. Mahmoud, P. Shi and A. Ismail, Robust Kalman filtering for discrete-time Markovian jump systems with parameter uncertainty, J. Computational and Applied Mathematics, vol.169, no.1, pp.53-69, 2004.
- [16] P. Shi, E. K. Boukas and R. Agarwal, Kalman filtering for continuous-time uncertain systems with Markovian jumping parameters, *IEEE Trans. on Automatic Control*, vol.44, no.8, pp.1592-1597, 1999.
- [17] P. Shi, M. Karan and Y. Kaya, Robust Kalman filter design for Markovian jump linear systems with norm-bounded unknown nonlinearities, *Circuits Systems and Signal Processing*, vol.24, no.2, pp.135-150, 2005.
- [18] X. Yao, S. Jun, M. Yang and R. Zhong, A new two-stage Kalman filter method for chaos system, *ICIC Express Letters*, vol.4, no.2, pp.539-546, 2010.
- [19] C. Lin, C. Yu, C. Lu, Y. Chung and T. Chen, Applying Kalman filter-based fusion algorithm to estimation problems, *ICIC Express Letters*, vol.4, no.6(A), pp.2109-2114, 2010.
- [20] C. Antoniou, M. B. Akiva and H. N. Koutsopoulos, Nonlinear Kalman filtering algorithms for on-line calibration of dynamic traffic assignment models, *IEEE Transactions on Intelligent Transportation* Systems, vol.8, no.4, pp.661-670, 2007.
- [21] M. Boutayeb and D. Aubry, A strong tracking extended Kalman observer for nonlinear discrete-time systems, *IEEE Transactions on Automatic Control*, vol.44, no.8, pp.1550-1556, 1999.
- [22] I. A. Hameed, Using the extended Kalman filter to improve the efficiency of greenhouse climate control, International Journal of Innovative Computing, Information and Control, vol.6, no.6, pp.2671-2680, 2010.
- [23] S. Julier, J. Uhlmann and H. F. D. Whyte, A new method for nonlinear transformation of means and covariances in filters and estimators, *IEEE Transactions on Automatic Control*, vol.45, no.3, pp.477-482, 2000.
- [24] S. Clark, Autonomous Land Vehicle Navigation Using Millimetre Wave Radar, Ph.D. Thesis, University of Sydney, Australia, 1999.
- [25] Y. He, J. J. Xiu and J. W. Zhang, Radar Data Processing with Applications, Electronics Industrial Press, Beijing, 2006.
- [26] A. Montobbio, Sperimentazione ed Affinamento di un Localizzatore, Ph.D. Thesis, Politechnico di Torino, Italy, 1998.
- [27] S. J. Julier and J. K. Uhlmann, A General Method for Approximating Nonlinear Transformations of Probability Distributions, Robotics Research Group, Department of Engineering Science, University of Oxford, 1994.
- [28] M. Tchamitchian and H. J. Tantau, Optimal control of the daily greenhouse climate: Physical approach, Proc. of the 13th IFAC World Congress, San Francisco, USA, pp.471-475, 1996.
- [29] O. Jolliet, HORTITRANS, a model for predicting and optimizing humidity and transpiration in greenhouses, *Journal of Agricultural Engineering Research*, vol.57, no.1, pp.23-37, 1994.
- [30] S. J. Julier and J. K. Uhlmann, A new extension of the Kalman filter to nonlinear systems, The 11th Int. Symp. on Aerospace/Defence Sensing, Simulation and Controls, 1997.